

ICL CIPHERS: Quantifying "Learning" in In-Context Learning via Substitution Ciphers

Zhouxiang Fang, Aayush Mishra, Muhan Gao, Anqi Liu, Daniel Khashabi

Presented by Zhouxiang Fang



Definition: In-context Learning (ICL) is an emerging feature of Large Language Models that allows them to identify patterns in demonstrations given as prompts and apply these patterns to similar tasks. ¹



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Changes of parameters are not needed when adapting to different tasks.



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Demonstrations

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Input: I love my school! There is ...
Output: positive
Input: The sky doesn't looks so nice
Output: negative
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    Output: positive
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Input: I don't love looking at the sky
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Literatures suggest that ICL operates in dual modes^{1,2}

^{2.}Lin, Ziqian, and Kangwook Lee. "Dual operating modes of in-context learning." *Forty-first International Conference on Machine Learning*. 2024.



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Literatures suggest that ICL operates in dual modes^{1,2}

- Task Retrieve (TR): Recall learned patterns from pre-training
- Task Learning (TL): Learning from demonstrations during inference time

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- Task Retrieve (TR): Recall learned patterns from pre-training
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Challenge: It's non-trivial to disentangle these two modes

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Sentiment Classification

Input: The weather is so good!

Output: positive

Input: I don't like that movie.

Output: negative

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TR

I've seen this task! It's sentiment classification.





Sentiment Classification

Input: The weather is so good!

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Input: 10 and 11

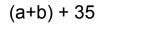
Output: 49 Input: 5 and 8 Output: 46

...



I've seen this task! It's sentiment classification.





 $(a*b + 2025) \mod$



Sentiment Classification

Input: The weather is so good!

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 $(a*b + 2025) \mod (a+b) + 35$

Input: 10 and 11

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...

TR

I've seen this task! It's sentiment classification.



I never see this task. Let me try to solve it by observing more demos.





TR:

Randomize the labels



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Input: I love my school! There is ...
Output: positive
Input: The sky doesn't look so nice
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Input: I don't love looking at the sky
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TR:

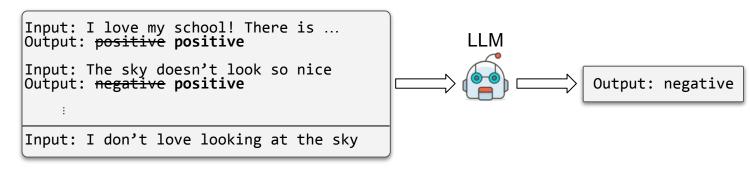
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TR:

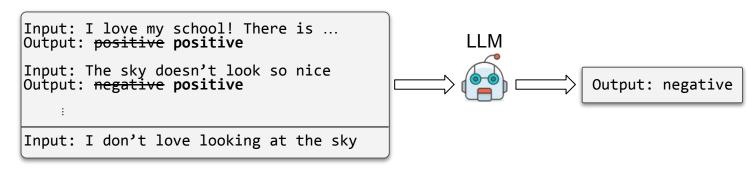
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TR:

Randomize the labels



TL:

Replacing the original labels with new labels



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Randomize the labels

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Input: I love my school! There is ...
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Input: I don't love looking at the sky

LLM
Output: negative
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TL:

Replacing the original labels with new labels

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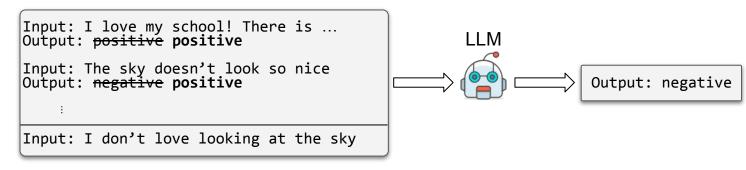
```
Input: I love my school! There is ...
Output: positive *
Input: The sky doesn't look so nice
Output: negative A

Input: I don't love looking at the sky
```



TR:

Randomize the labels



TL:

Replacing the original labels with new labels

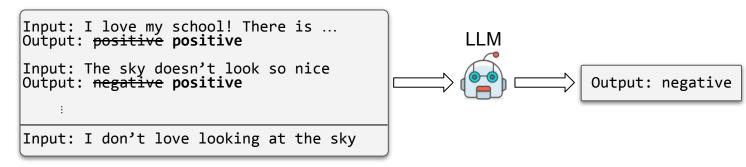
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Output: A
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High-level Idea and Solution



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High-level idea:

- 1. Create a task that is rather **unlikely to be included** during pre-training
- 2. See if LLMs can solve the task via ICL **Evidence for TL**



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High-level idea:

- 1. Create a task that is rather **unlikely to be included** during pre-training
- 2. See if LLMs can solve the task via ICL **Evidence for TL**

Solution:

ICL ciphers - a class of task reformulations based on substitution ciphers





What is a substitution cipher?

- It is a method of encrypting in which **units** of plaintext are replaced with the ciphertext, in a defined manner (mapping)



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e.g. Caesar cipher is one kind of classic substitution cipher





What is a ICL cipher?

- A token-level substitution cipher, applied to ICL inputs



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Two types of ICL cipher

- Bijective Cipher: A reversible framework, where a bijective mapping between original tokens and encoded tokens is maintained
- Non-bijective Cipher: An **non-reversible** framework, where such bijective mapping doesn't exist



What is a ICL cipher?

- A token-level substitution cipher, applied to ICL inputs

Two types of ICL cipher

- Bijective Cipher: A reversible framework, where a bijective mapping between original tokens and encoded tokens is maintained
- Non-bijective Cipher: An **non-reversible** framework, where such bijective mapping doesn't exist

We use the performance gap between Bijective and Non-bijective Cipher to quantify TL



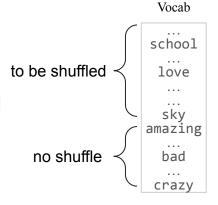
Original Vocab

school
...
love
...
sky
amazing
...
bad
...
crazy



Bijective Cipher:

1. Pick a shuffle rate **r** from 0 to 1, then choose **r** * **Vocab size** tokens to be shuffled

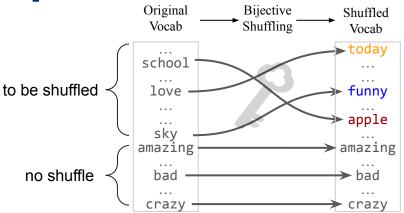


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Bijective Cipher:

- 1. Pick a shuffle rate **r** from 0 to 1, then choose **r** * **Vocab size** tokens to be shuffled
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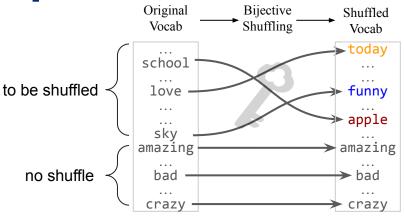


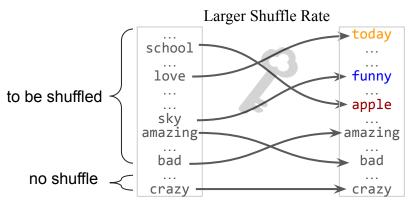


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Larger shuffle rate means more tokens are shuffled

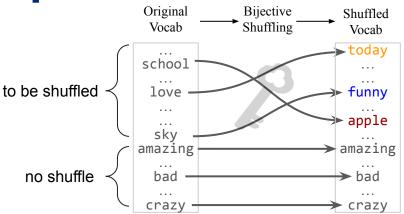






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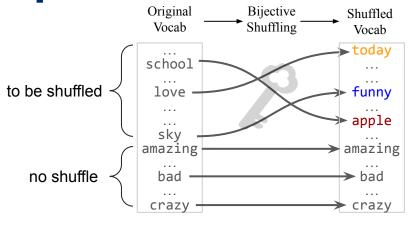


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3. Replace tokens in the input text according to the bijective mapping



In-Context Learning

Input: I love my school! There is
...
Output: positive
Input: The sky doesn't look so nice
Output: negative

Input: I don't love looking at the sky

Ciphered In-Context Learning

Input: I love my school! There is
...
Output: positive
Input: The sky doesn't look so nice
Output: negative
...
Input: I don't love looking at the sky

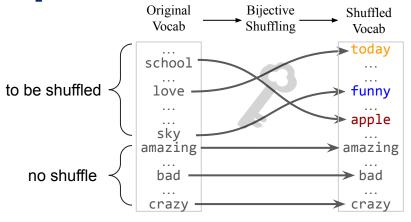


Bijective Cipher:

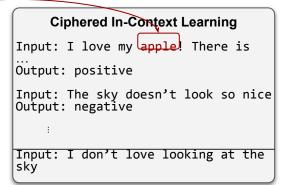
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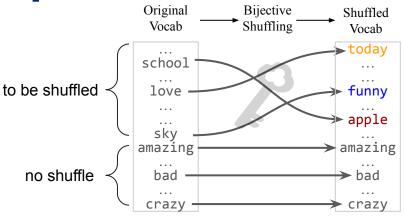


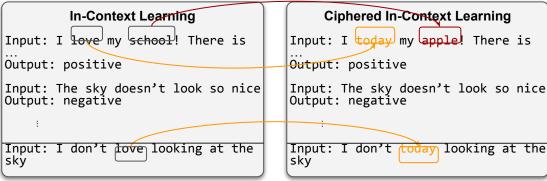
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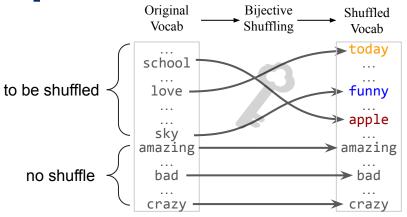


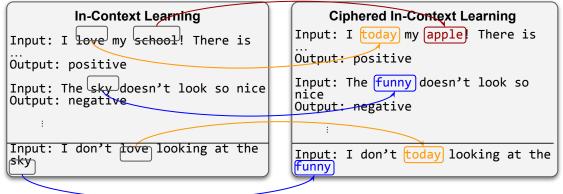
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Non-bijective Cipher:

1. Conduct replacing on the same tokens as bijective cipher



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In-Context Learning Input: I love my school! There is ... Output: positive Input: The sky doesn't look so nice Output: negative

Input: I don't love looking at the sky



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- 1. Conduct replacing on the same tokens as bijective cipher
- 2. For each token that should be ciphered (replaced), replace it with a randomly selected token

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Input: I love my school! There is ...
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Ciphered In-Context Learning
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In-Context Learning
Input: I love my school! There is ...
Output: positive
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Output: negative
...
Input: I don't love looking at the sky
```

```
Ciphered In-Context Learning
Input: I love my shaking! There is ...
Output: positive

Input: The sky doesn't look so nice
Output: negative

Input: I don't love looking at the sky
```



- 1. Conduct replacing on the same tokens as bijective cipher
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Input: I love my school! There is ...
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Output: negative

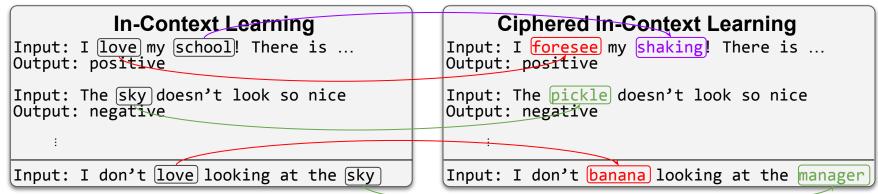
Input: I don't love looking at the sky

Ciphered in-Context Learning
Input: I foresee my shaking! There is ...
Output: positive

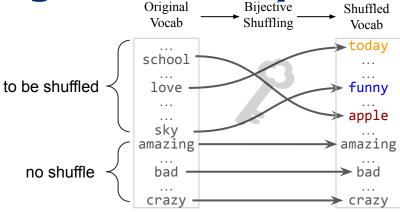
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Output: negative

Input: I don't banana looking at the sky
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Quantifying "Task Learning" via ICL Ciphers Original Shuffled





Quantifying "Task Learning" via ICL Ciphers

Original Vocab Shuffling Vocab school Original (plain) text: I **love** my cats and they **love** me back. to be shuffled love funnv apple Bijective Cipher: I today my cats and they today me back. sky amazing amazing Non-bijective Cipher: I pickle my cats and they share me back. no shuffle bad ► bad crazy crazy



Quantifying "Task Learning" via ICL Ciphers

Original (plain) text: I **love** my cats and they **love** me back.

Bijective Shuffled Vocab

Coriginal Vocab

Shuffled Vocab

Coriginal Vocab

Shuffled Vocab

Coriginal Vocab

Shuffled Vocab

Working Hypothesis:

The **bijective mappings** between original and shuffled vocabs ensures bijective ciphers are **reversible and learnable**, while non-bijective ciphers are **non-reversible and unlearnable** as their replacement process don't follow the bijective mapping



Quantifying "Task Learning" via ICL Ciphers

Original Vocab

Original Vocab

Shuffled Vocab

Original Vocab

Shuffled Vocab

Today

School

School

School

Solution

School

Solution

School

Solution

Two ciphers conduct replacement on same tokens. Therefore, the performance gap between them only comes from the way of ciphering, which reflects how much the LLM learns about the bijective mapping — Quantified evidence of TL!

Note that LLMs are not required to fully "deciphering" the ciphers, but only need to (internally) capture related information or attributes (e.g. sentiment) of the ciphered tokens that help solve the reformulated tasks. — The reformulated tasks are different!



$Model \to$	Cipher	20-shot					
Dataset (shuffle rate) \downarrow	O-P-IO-I	Llama3.1	Qwen2.5	Olmo	Gemma2		
SST-2 $(r = 0.5)$	Non-Bijective Bijective	58.3 63.1 (+4.8 ↑)*	69.0 73.5 (+4.5 ↑)*	67.7 72.7 (+5.0 \(\gamma\))*	70.5 74.2 (+3.7 ↑)*		

Green: Gain

Red: Loss



$Model \to$	Cipher		20-shot				
Dataset (shuffle rate) ↓		Llama3.1	Qwen2.5	Olmo	Gemma2		
Amazon $(r=0.6)$	Non-Bijective Bijective	64.7 72.3 (+7.6 ↑)*	72.6 77.9 (+5.3 ↑)*	77.2 80.2 (+3.0 ↑)*	80.8 85.0 (+4.2 ↑)*		
	BREGIT	7210 (1710 [)	776 (1616)	(1010)	(, ,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,		
Croons Cain	Dod. Lo	CC	* Ctatictic	sally cianifi	cant		

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$Model \to$	Cipher	20-shot					
Dataset (shuffle rate) ↓	2277 (Llama3.1	Qwen2.5	Olmo	Gemma2		
HellaSwag ($r = 0.3$)	Non-BIJECTIVE	29.7	52.8	25.9	37.1		
Tienaswag ($t = 0.5$)	BIJECTIVE	$31.9 (+2.2 \uparrow)^*$	$62.3 (+9.5 \uparrow)^*$	$26.1 (+0.2 \uparrow)^*$	$36.6 (-0.5 \downarrow)$		

Green: Gain

Red: Loss



$Model \to$	Cipher	20-shot					
Dataset (shuffle rate) ↓	Saff star Providence	Llama3.1	Qwen2.5	Olmo	Gemma2		
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WinoGrande ($r = 0.1$)	Non-Bijective	53.7	61.3	53.4	63.5		
	Bijective	55.5 (+1.8 ↑)*	62.5 (+1.2 ↑)	53.1 (-0.3 ↓)	63.5 (+0.0 ↑)		

Green: Gain

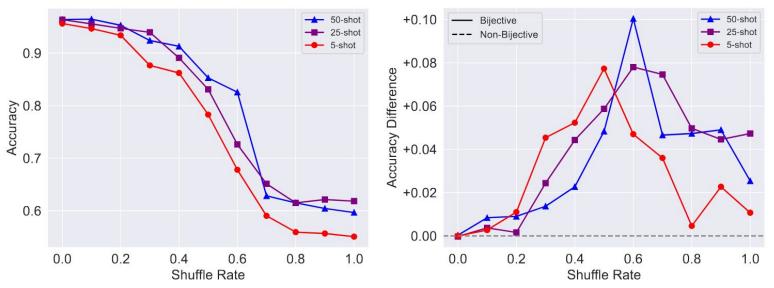
Red: Loss

*: Statistically significant

Consistent **gaps** between bijective and non-bijective ciphers across different **models and datasets**, demonstrating LLMs are able to solve the bijective cipher via ICL — evidence for TL.



Results: Performance decreases as shuffle rate increase



As shuffle rate increases, the accuracy drops but remain above random. The gap first increases to a certain peak (r=0.6) then decreases



Results: Gaps increase with more demonstrations

Shots \rightarrow	Cipher	/		Model: I	Llama 3.1 8B		
Dataset (shuffle rate)↓	Сірпеі	5-shot	10-shot	15-shot	20-shot	25-shot	50-shot
SST-2 $(r = 0.5)$	Non-BIJECTIVE BIJECTIVE	56.9 59.5 (+2.6 ↑)*	59.5 61.0 (+1.5 ↑)	58.6 60.8 (+2.2 ↑)	58.3 63.1 (+4.8 ↑)*	62.6 65.4 (+2.8 ↑)*	58.4 64.9 (+6.5 ↑)*

Green: Gain

Red: Loss



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Green: Gain

Red: Loss



Results: Gaps increase with more demonstrations

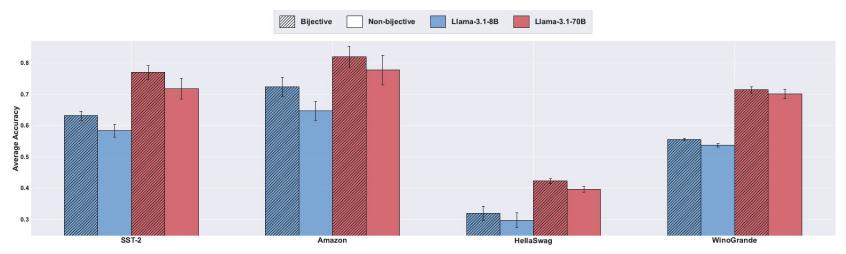
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Green: Gain Red: Loss *: Statistically significant

The gap between bijective and non-bijective ciphers increases as few-shot number grows



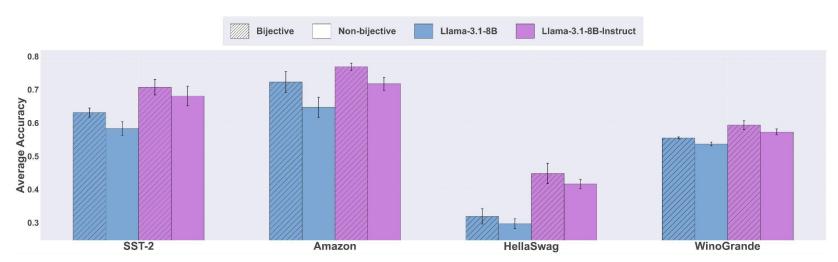
Results: Larger model has on-par gaps with smaller model



The gaps between bijective and non-bijective ciphers exist in **larger model**, on-par with smaller model



Results: Mixed gap difference between aligned/pretrained models



The aligned model has better absolute performance.

The differences in gaps for pretrained and aligned models are mixed.





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Gaps exist across models and datasets — Evidence for TL



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- Future work:

- 1. More models/datasets/interpretability analysis
- 2. Different levels of ciphering (e.g. word)

